

Addition

Progression towards a formal written method:

$47 + 25 =$

47 + 25 = 60 + 12

Addition starts very practically using straws then dienes. Children use knowledge of place value to make the numbers and then add them together before exchanging when there are 10 1's.

Leading to exchanging:

72

100 100	10 10 10 10	1 1 1 1 1 1 1
100	10 10	1 1 1 1 1

$$\begin{array}{r}
 200 + 40 + 7 \\
 100 + 20 + 5 \\
 \hline
 300 + 60 + 12 = 372
 \end{array}$$

Children partition their numbers horizontally and add each place value column (starting with the ones) continuing to use resources for support (straws, dienes and then place value counters).

100 100 100	10 10 10 10 10 10	1 1 1 1 1 1 1 1 1 1
-------------------	-------------------------	---------------------------------

$$\begin{array}{r}
 247 \\
 +125 \\
 \hline
 12 \\
 60 \\
 300 \\
 \hline
 372
 \end{array}$$

Children then use the expanded vertical method continuing to focus on place value and adding their ones first. Children continue to use practical resources alongside this to support understanding.

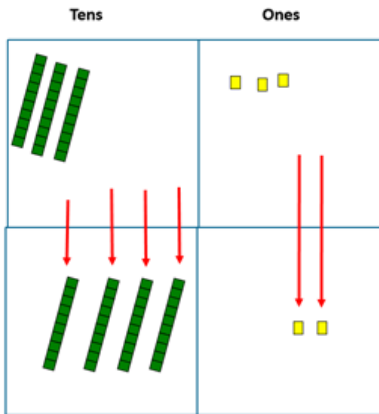
• •	••••	•••	••
••••	••••	•	••••
7	1	5	1
•		•	

$$\begin{array}{r}
 2634 \\
 +4517 \\
 \hline
 7151 \\
 \hline
 \quad 1 \quad 1
 \end{array}$$

Finally children use the formal written method for addition lining their numbers up vertically and exchanging underneath when required.

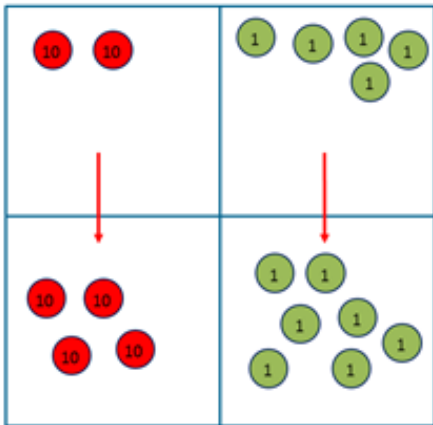
Subtraction

Progression towards a formal written method:



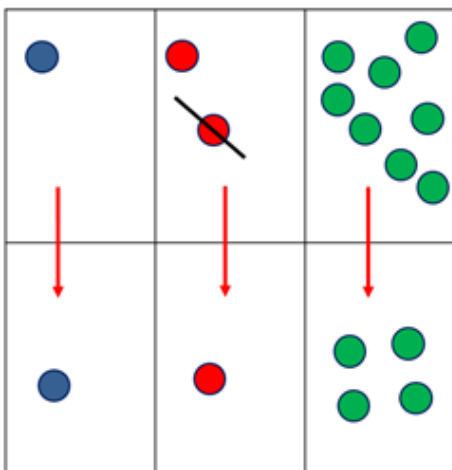
$$\begin{array}{r} 70 \quad 5 \\ - 40 \quad 2 \\ \hline 30 \quad 3 \end{array}$$

Subtraction starts practically using straws then dienes. Children learn that they only need to make the top number and that they have to subtract the bottom number from this. They learn to write this expanded horizontally using place value columns.



$$\begin{array}{r} \overset{60}{\cancel{70}} \quad \overset{1}{2} \\ - 40 \quad 7 \\ \hline 20 \quad 5 \end{array}$$

This progresses to questions where children will need to exchange. Again, children start by doing this practically to reinforce the understanding that a 10 is the same as 10 1's. They learn how to record this by crossing out and exchanging to the 10.

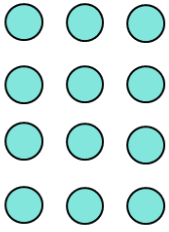


$$\begin{array}{r} \overset{2}{\cancel{2}} \overset{1}{\cancel{3}} \quad 2 \\ - 114 \\ \hline 118 \end{array}$$

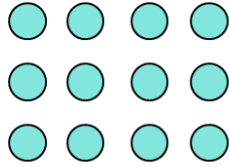
When children are secure with their place value they no longer need to expand the method horizontally by partitioning and use the formal written method for subtraction. Numbers are lined up vertically in the correct columns and exchanging is marked without place value.

Multiplication

Progression towards a formal written method:

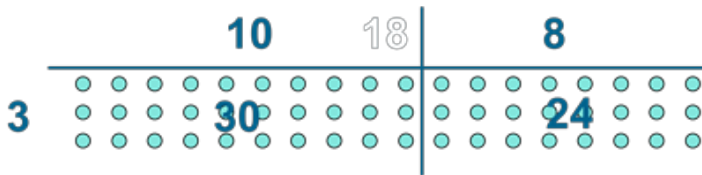


$$3 \times 4$$

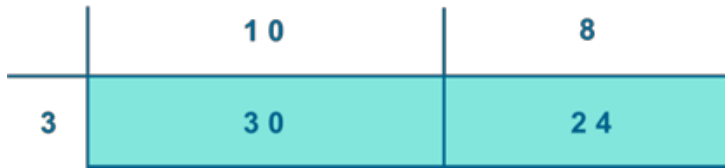


$$4 \times 3$$

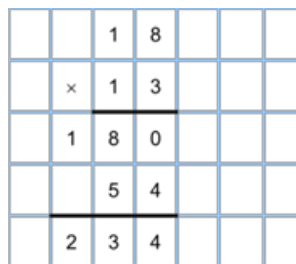
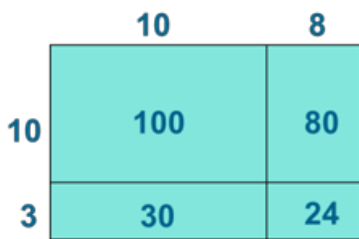
Children use arrays as a visual to represent multiplication. These can be done practically as well as written. Children understand that multiplication is the same as repeated addition and that 3 multiplied by 4 and 4 multiplied by 3 give the same answers.



The array is used to represent multiplication with larger numbers so children understand the place value involved.



This leads clearly into the grid method where children partition each of the numbers they are multiplying and write the answers to each calculation within their grid.

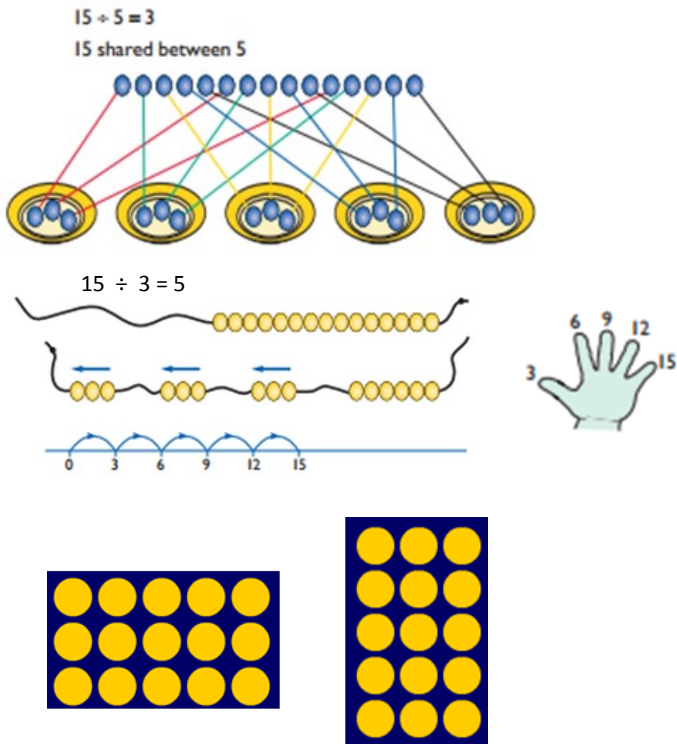


The grid method continues to be used with larger numbers and when children are confident and secure they are moved onto the formal written method for multiplication. Children are encouraged to see the connections between the grid and formal methods. As this gets more difficult, the children show their exchanging above and below the numbers.

$$\begin{array}{r}
 \begin{array}{cccc}
 & 2 & 3 & 1 \\
 & 1 & 3 & 4 & 2 \\
 \times & & 1 & 8 & \\
 \hline
 1 & 3 & 4 & 2 & 0 \\
 1 & 0 & 7 & 3 & 6 \\
 \hline
 2 & 4 & 1 & 5 & 6 \\
 \hline
 & & & & 1
 \end{array}
 \end{array}$$

Division

Progression towards a formal written method:



Children look at division as sharing and grouping. When children share they use objects to share practically. When grouping, children apply their counting skills using practical resources, their fingers or a number line.



Children make links between multiplication and division using arrays.

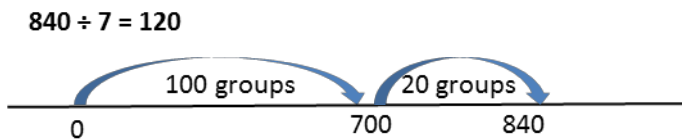
E.g.

$15 \div 3 = 5$ there are 5 groups of 3

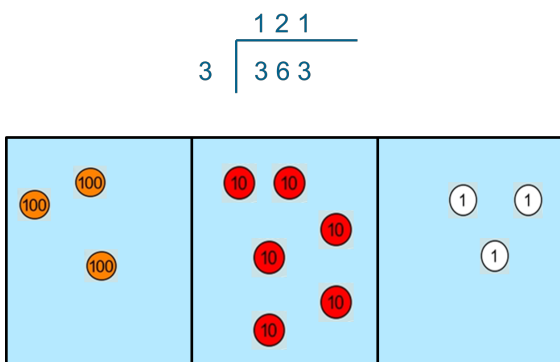
$15 \div 5 = 3$ there are 3 groups of 5



Children continue to develop grouping on a number line using their times tables facts to work with larger numbers. They learn to look for groups of the divisor e.g. 10 groups of, 100 groups of. Calculations may have remainders.



Children learn to use the formal method alongside place value counters or dienes. They continue to use grouping within this method e.g. How many groups of 3 can I make in the hundreds?

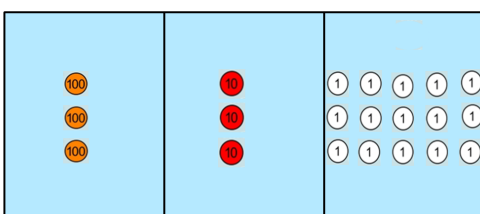


$345 \div 3 =$

$3 \overline{) 345}$

1 1 5

National Centre
for Excellence in the
Teaching of Mathematics



Children continue to develop their use of the formal method where questions involve exchange.